



Efficient Trichromatic Nd:YLF Laser Emitting at 1047 nm, 1053 nm and 1314 nm

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Abstract: We report a Nd:YLF laser, side-pumped by a diode-stack at 797 nm with 1545 W peak power, resulting in triple-wavelength emission at 1314 nm, 1053 nm, and 1047 nm. The resonator is capable of emitting each wavelength separately as well as any combination of them simply by cavity alignment. When operating at 1314 nm, the laser reached record optical-to-optical efficiency of 49%, with a slope efficiency of 53%.

Keywords: Nd:YLF; solid-state Laser; multichromatic emission; trichromatic laser; triple-wavelength; 1314 nm; 1053 nm; 1047 nm

1. Introduction

Nd-doped crystals have demonstrated simultaneous laser emissions at different wavelengths, a property known as multichromatic emission. This can be observed for 1053 nm and 1047 nm emission from a Nd:YLF laser, or more distant emissions, such as 1064 nm and 1342 nm or 1064 nm and 946 nm for Nd:YAG lasers [1,2]. One of the remarkable features of multichromatic lasers is their ability to access multiple absorption lines of various materials. One notable application in this regard is Laser-Induced Breakdown Spectroscopy (LIBS). In this process, a short-to-ultrashort laser pulse turns a tiny fraction of a material sample into plasma for spectral analysis, thus avoiding extensive sample preparation. This technology can be used for several processes, including environmental monitoring through rapid analysis of air, soil sewage sludge, and wastewater, material analysis in the metal industry, and in mining as a tool for establishing ore composition [3].

Multichromatic lasers can also be applied in coating inspection [4], depth-resolved measurement of element composition [5], and microwave and terahertz generation [6,7]. Additionally, the frequency of the emitted beams can be doubled or tripled through second and third harmonic generation (SHG and THG), leading to green, red, and blue emissions that are interesting for applications in Light Detection and Ranging (LIDAR) and range finding [2,8,9]. These emissions can be Raman shifted before frequency double, leading to interesting medical applications such as retinal photocoagulation [10,11].

Amongst Neodymium (Nd)-doped crystals, which are well known for their 1 μ m emissions, Yttrium Aluminum Garnet (Nd:YAG) and Yttrium Orthovanadate (Nd:YVO) emitting at 1064 nm, and Yttrium Lithium Fluoride (Nd:YLF), emitting at both 1053 nm (σ) and 1047 nm (π), are most commonly used [12–14]. Recently grown crystals, such as Lutetium Aluminum Garnet (Nd:LuAG), have also garnered interest for potential new applications, especially for the generation of Q-switched pulses with saturable absorbers [15].

Emissions at 1 μ m are favored for efficient high-power lasers due to their greater emission cross-section. Emissions at 1.3 μ m can be particularly advantageous when Ramanshifted, as their proximity to the 1.4 μ m region makes them suitable for lower-cost eye-safe lasers and applications such as free space communications [16,17].



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Copyright: © 2023 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). While Nd:YVO and Nd:YAG exhibit higher emission cross-sections compared to the Nd:YLF, they are more susceptible to thermal effects and have shorter lifetimes. Nd:YLF, in contrast, boasts twice the upper-state lifetime of Nd:YAG and nine times that of Nd:YVO, making it an excellent choice for high-power and Q-Switched operations, especially in a side-pumping configuration for a better pump-power density distribution, reduced thermal lensing, and, consequently, greater output power [18,19]. Additionally, Nd:YLF emits at 1.31 μ m, distinguishing it from Nd:YAG and Nd:YVO, which emit at around 1.34 μ m, making it suitable, for example, as a local oscillator for the optical atomic calcium clock [20].

The double-wavelength emission of an Nd:YLF laser at the 1.05 μ m and 1.31 μ m regions was first demonstrated in 1983 [21]. However, its lamp-based pumping scheme significantly restrained efficiency. Diode-pumping overcomes this issue due to the narrow emission bandwidth of common diode lasers (<3 nm), and it is further enhanced by the use of technologies, such as volume Bragg gratings (VBG), for an even narrower emission (<0.5 nm) [22]. In 2001, Damzen et al. achieved a 75% slope efficiency and 64% conversion efficiency with diode-pumped Nd:YVO lasers in grazing-incidence singlebounce resonators. In this configuration, the laser beam undergoes a total internal reflection (TIR) at the crystal's pump face, exposing the intracavity beam's peak intensity to the area of the highest population inversion. These results were essential to establish this cavity design as an excellent alternative to highly efficient side-pumped configurations [23,24]. Recently, single-bounce resonators yielded the record-breaking slope efficiency of 68% for an Nd:YLF diode-pumped at 797 nm, although it has failed to attain a diffraction-limited output beam [25,26]. An intriguing strategy to balance efficiency and high-beam quality in these side-pumped resonators involves the incorporation of a third folding mirror within the cavity. This addition results in two, close-to-parallel laser beams undergoing both total internal reflection at the pump face of the crystal. Controlling the distance between these laser beams within the crystal diminishes the oscillation of higher-order modes, leading to a TEM₀₀ output beam. This approach has been named the Double-Beam Mode Controlling Cavity (DBMC) [22,27]. It has been effectively implemented for laser emissions at 1053 nm and 1314 nm. At 1053 nm, this approach achieved a slope efficiency of 65% with TEM₀₀ emission [22], while at 1314 nm, with its smaller cross-section, slope efficiencies of 54% and optical-to-optical efficiencies of 34% have been achieved with 792 nm pumping [28].

Single-bounce resonators can achieve diffraction-limited beam quality alongside remarkable efficiency values. In 2022, a side-pumped Nd:YLF laser achieved a near-quantum defect slope efficiency of 78% by directly pumping at the 863 nm wavelength. A planeplane resonator was employed to reconcile this efficiency achievement with the desired TEM₀₀ laser beam, incorporating intracavity cylindrical lenses to mitigate diffraction losses at the crystal's borders [29,30]. These single-bounce cavities are especially interesting for passively Q-switching laser applications. Their inherent simplicity aligns seamlessly with the ease of integrating a saturable absorber in the laser cavity. Furthermore, their compact nature facilitates the generation of shorter pulses without compromising energy capabilities, favoring higher peak power emissions. Recent work in 2023 showcased a Cr:YAG/Nd:YLF laser within a compact single-bounce cavity, achieving a peak power of 46 MW coupled with a pulse energy of 41 mJ. Notably, this configuration set a new benchmark for energy per pulse in passively Q-switched Nd:YLF lasers and demonstrated Q-switched dual-wavelength laser beams at 1047 nm and 1053 nm wavelengths [31].

The importance of efficient triple-wavelength emission lies in its potential to open doors to a wider array of laser applications, particularly in the generation of diverse wavelengths through phenomena such as second harmonic generation (SHG), sum- and difference frequency generation (SFG and DFG). This capability not only enriches the versatility of these lasers, but also expands their utility across various fields. A diverse range of Nd³⁺-doped lasers have demonstrated the ability to emit triple-wavelength (multichromatic) emissions, with Nd:YGG emitting at 1062 + 1060 + 1058 nm [32], Nd:SYSO emitting at 1075 + 1076 + 1078 nm [33], Nd:YVO emitting at 1062 + 1064 + 1066 nm [34], and Nd:YAG with emissions of 1064 + 1319 + 1338 nm or even at 469 + 471 + 473 nm via frequency

doubling and sum-frequency mixing [35,36]. So far, however, Nd:YLF lasers have only presented double-wavelength emission, such as 1314 + 1321 nm [37], 1047 + 1053 nm [38], and 1047 + 1314 nm [21], presenting trichromatic emission only through the use of nonlinear effects.

To the best of our knowledge, this work demonstrates the first fundamental, triplewavelength emission of a Nd:YLF crystal. The presented laser displays efficient multichromatic emissions at combinations of 1047 nm, 1053 nm, and 1314 nm. Each wavelength operation can be selected by simple cavity alignment, allowing for a single, double, or triple-wavelength emission. This design reached efficiencies above 31% for all wavelength operations, achieving record values for slope- and optical-to-optical efficiency at 1314 nm with 797 nm pumping.

2. Materials and Methods

A VBG-equipped 12-bar diode stack (Northrop Grumman, St. Charles, MO, USA), with 1544.8 \pm 8.8 W peak power, was employed to side-pump a 13 \times 13 \times 3 mm³, a-cut, Nd:YLF crystal (Crystech, Qingdao, China), with 1 mol% Nd³⁺ doping. The pumping duty cycle of 0.17% (350 µs; 5 Hz) was set by the manufacturer to maintain the 797 nm emission line at a measured width of 0.92 \pm 0.03 nm at Full Width at Half Maximum (FWHM). The pump diode's emission was focused by a doublet lens (D), with f = 30 mm, to guarantee good spatial overlap between pump- and laser beams. A half-wave plate (HP) was employed to set the polarization of the pump diode to be parallel to the c-axis of the crystal, improving absorption.

The resonator configuration used a total internal reflection at the pump facet of the crystal to expose the center of the TEM₀₀ mode (the peak intensity of the intracavity beam) to the area of highest population inversion. A Brewster's angle of incidence ($\Theta_B = 55.4^\circ$ for the σ -transition) was employed at the uncoated lateral faces of the crystal for the intracavity beam to achieve wavelength emission at 1314 nm (σ -polarized) and to reduce Fresnel reflection losses.

Due to its significantly lower emission cross-section at 1.31 μ m, laser emission requires the employment of mirrors with high transmittance at 1.05 μ m. Therefore, a plane output coupler (M1), with transmissions of T_{-1.31 μ m} = 10% and T_{-1.05 μ m} = 75%, and a highly reflective (HR) concave mirror at 1.31 μ m (M2), with a radius of curvatures (ROC) of 8 m and T_{-1.05 μ m} = 92%, were used to achieve emission of 1314 nm. In this two-mirror configuration, the reflection of M1 and M2 in the 1.05 μ m region is still sufficient for 1047 nm oscillation when at least one of the laser mirrors is slightly misaligned to impede 1314 nm oscillation. The misalignment effectively diminishes reflectivity at 1314 nm, increasing the resonator's tendency to oscillate at the 1.05 μ m region due to its larger emission crosssection, as shown in Table 1.

	⁴ F _{3/2} –	$ ightarrow {}^{4}I_{11/2}$	$^4\mathrm{F}_{3/2} ightarrow ^4\mathrm{I}_{13/2}$		
	1047 nm (π)	1053 nm (σ)	1321 nm (π)	1314 nm (σ)	
$\sigma_{\rm e}~(10^{-19}~{\rm cm}^2)$	1.8	1.2	0.27	0.33	

Table 1. Nd:YLF stimulated emissions cross sections at 1047, 1053, 1321, and 1314 nm [18,39].

The low reflectivity of both mirrors at 1.05 μ m, together with the lower emission crosssection of the 1053 nm wavelength, favors the oscillation of the π -polarized wavelength of 1047 nm, despite the use of a Brewster angle of incidence for the σ -transition. Therefore, to achieve 1053 nm wavelength emission, a 1.05 μ m HR plane mirror (M3) was added behind the M2 mirror, as shown in Figure 1A.



Figure 1. (**A**): Single-bounce resonator configuration. M1, M2, and M3 are laser mirrors; D is a doublet with a 30 mm focal distance; HP is a half-wave plate. (**B**): Diagram of the relevant energy transitions in Nd:YLF [40,41].

Figure 2 presents the transmittance spectrum, measured by a Varian CARY[®] 5000 spectrometer (Agilent Technologies, Santa Clara, CA, USA), of all three mirrors utilized in the laser resonator.



Figure 2. Spectrum of laser mirrors (950 nm to 1350 nm). (**A**): Transmission of M1. (**B**): Transmission of M2. (**C**): Transmission of M3.

The cavity length between M1 and M2 was set to 140 mm, resulting in a (simulated; LASCAD v. 3.6) mode spot radius inside the crystal of 1983 μ m \times 1148 μ m in the horizontal and vertical directions, respectively, using the M^2 beam quality factor, shown in Figure 6 (measured for the σ -transition of 1314 nm. The cavity length between M1 and M3 was set to 180 mm, resulting in a spot size (radius) of 1931 μ m \times 1275 μ m in the horizontal and vertical directions, respectively. It should be noted that the larger horizontal dimension is caused by two factors, the Brewster angle of incidence at the crystal's side facets and the larger M^2 beam quality factor in the horizontal direction. With a measured pump spot size of $2100 \pm 250 \ \mu\text{m} \times 145 \pm 30 \ \mu\text{m}$, we guarantee good spatial overlap by focusing the pump light into a smaller spot size at the crystal's pump surface than the area of the TIR of the simulated laser mode, especially in the vertical direction. We remark that because of Brewster angle of incidence of the laser mode at the TIR surface inside the crystal, the beam size in the pump direction is an additional n times larger (n being the refractive index of the σ -transition) than the mode spot size inside the crystal. Therefore, the overlap integral benefits from the geometry of this set-up is responsible for an n² -times larger laser beam mode in the pump direction. Specifically in the above case, the $1/e^2$ mode size in the pump direction is 5.75 mm for the M1–M2 cavity.

The spectral overlap was calculated with a MatLab script in which, in the first step, convolutes the emission curve of the pump diode with the absorption spectrum of the Nd:YLF crystal with 1% doping, shown in Figure 3A,B, respectively. As a result, the effective absorption coefficient decreases non-exponentially as a function of the absorption

depth inside the crystal, because the diode's frequencies closest to its emission peak are more efficiently absorbed by the crystal's narrow absorption peak if both spectra overlap perfectly, when compared to frequencies farther away from the diode's emission peak. Figure 3C displays the effective absorption as a function of the pump depth. The absorption at 5.75 mm is higher than 97%. The effective absorption coefficient needs to be considered in order to calculate the overall overlap efficiency below (Equation (1)).



Figure 3. (**A**): Emission spectrum of 797 nm diode stack, measured by a HR2000 spectrometer (OceanInsight, Orlando, FL, USA) with 0.24 nm resolution at FWHM; (**B**): Absorption spectrum of Nd:YLF, measured by a Varian CARY[®] 5000 spectrometer. (**C**): Effective absorption in function of the pump depth.

In agreement with the theory of Kubodera et al. [42], the total overlap efficiency of the system can be defined as the integral of the spatial, normalized population inversion saturated by the oscillating field, also called remaining inversion, divided by non-saturated inversion.

$$\iiint \frac{r_0(x,y,z)}{1+\sum_j S_j s_{0j}(x,y,z)/I_0} dv / \iiint r_0(x,y,z) dv$$
(1)

where dv is integrated over the pump volume, I₀ is the saturation intensity, S_j the photon number in TEM mode j, s_{0j} and r_0 the normalized distribution function of mode j and the pump mode, respectively. The Matlab script calculates which ressonator mode j enters oscillation first, under the condition of a specific pump distribution. From there on it calculates, for each pump power, the denominator in Equation (1) for the sum of all oscillating modes j and checks if another additional mode i can oscillate (reach threshold) at the same pump power R. The Matlab code then resolves the system of i non-linear equations and calculates the values of S_j for each mode, which is proportional to the fractional output power of each mode. The calculated resultant overlap efficiency is 98.3% for the 1314 nm transition.

Wavelength Selection

To comprehend the mechanism of selection of each wavelength, we first examine a resonator equipped with only two laser mirrors, M1 and M2. When both mirrors are precisely aligned, the laser cavity is optimized for single-wavelength operation at 1314 nm. This occurs due to both mirrors having high transmittance in the 1 μ m range and optimal reflectivity for 1314 nm. Since the ${}^{4}F_{3/2} \rightarrow {}^{4}I_{11/2}$ transition has a much larger emission cross-section compared to the ${}^{4}F_{3/2} \rightarrow {}^{4}I_{13/2}$ transition, emission at 1.05 μ m is achieved by intentionally disturbing the alignment of M2 for 1314 nm emission. This misalignment disrupts the conditions for 1314 nm emission, reducing the competition from 1314 nm and allowing the emergence of the 1047 nm wavelength. The transition from 1314 nm to 1047 nm, or vice versa, occurs gradually as we reduce alignment for the 1314 nm wavelength. As a result, we can achieve any combination of both wavelengths simultaneously just by controlling the alignment of the cavity's mirrors. Mirror M3 assumes a pivotal role by increasing reflectivity at 1.05 μ m, thereby enabling the emission of the 1053 nm wavelength and also enhancing efficiency at the 1.047 μ m transition. By adjusting the alignment of M3 and considering the 1047 nm losses induced by the Brewster angle of incidence, which causes an 8% reflection loss per surface for this wavelength, we can facilitate the emission

of either 1047 nm or 1053 nm, or even a combination of both simultaneously. Therefore, triple wavelength emission of 1047 nm, 1053 nm and 1314 nm is achieved by using main alignment of M3 for controlling the relative emission intensity of 1047 nm and 1053 nm while M2 controls the 1.3 μ m emission.

3. Results and Discussion

Figure 4 shows the spectrum of the laser emitting in single-wavelength operation at 1047 nm, 1053 nm, and 1314 nm in the dual-wavelength regime at 1047 nm and 1053 nm, 1047 nm and 1314 nm, 1053 nm and 1314 nm, and during triple-wavelength emission of 1047 nm, 1053 nm and 1314 nm. The 1047 nm and 1053 nm emissions were measured with a fiber-coupled (50 μ m fiber) high-resolution spectrometer (HR2000; Ocean Optics Inc., Orlando, FL, USA, 0.24 nm resolution at FWHM), yielding an emission line width at FWHM of 0.27 \pm 0.1 nm and 0.38 \pm 0.1 nm for 1047 nm and 1053 nm, respectively. The emission at 1314 nm was measured by a fiber-coupled InGaAs spectrometer (NIR quest; Ocean Optics Inc., 3.3 \pm 0.2 nm FWHM resolution) using a 10 μ m fiber.



Figure 4. Emission spectra of the Nd:YLF laser. (A): 1047 nm emission. (B): 1053 nm. (C): 1314 nm. (D): simultaneous emission of 1047 nm and 1053 nm. (E): 1047 nm and 1314 nm. (F): 1053 nm and 1314 nm. (G): 1047 nm, 1053 nm, and 1314 nm (resolution of 3.3 ± 0.2 nm).

Even at high-pump powers the laser did not present thermal lensing or any special cooling requirements due to the low duty cycle; the maximum average pump power was of the order of 2.7 W. Figure 5 shows the peak output power vs. the incident pump power after the 3.6% Fresnel losses at the pump face of the crystal for each of the three emission regimes of the laser cavity.



Figure 5. Peak output power vs. incident power for the emissions of: 1314 nm, 1053 nm, 1047 + 1053 + 1314 nm, 1053 + 1314 nm, 1047 + 1053 nm, 1047 + 1314 nm, and 1047 nm.

A slope efficiency of $52.8 \pm 0.7\%$ and an optical-to-optical efficiency of $48.6 \pm 0.3\%$ were achieved for the single wavelength emission at 1314 nm. To the best of our knowledge, this represents the highest optical-to-optical efficiency achieved at 1314 nm to date and the best slope efficiency for 797 nm pumping. When optimized for 1047 nm or 1053 nm emission, measured slope efficiencies were $34.7 \pm 0.9\%$ and $43.5 \pm 0.5\%$, respectively. Dualwavelength emission at 1047 + 1053 nm or at 1047 + 1314 nm resulted in slope efficiencies of $38.9 \pm 0.5\%$ and $31.5 \pm 0.5\%$, respectively, while 1053 + 1314 nm emission yielded a value of $41.1 \pm 0.4\%$. Finally, the triple-wavelength emission of 1047 + 1053 + 1314 nm presented a slope efficiency of $42.5 \pm 0.6\%$ and an optical-to-optical efficiency of 38.4 ± 0.3 . Table 2 presents the results of peak output power, pulse width, slope efficiency, and optical efficiency for each wavelength combination.

Table 2. Measured Nd:YLF monochromatic, bichromatic, and trichromatic laser results (* optical efficiency calculated from slope efficiency).

	Laser Emission Regime						
Nd:YLF Laser	1314 nm	1047 nm	1053 nm	1047 + 1053 nm	1047 + 1314 nm	1053 + 1314 nm	1047 + 1053 + 1314 nm
Peak Output Power (W) Pulse width (μs) Slope efficiency (%) Optical efficiency (%)	$\begin{array}{c} 726 \pm 3 \\ 342 \pm 0.1 \\ 53 \pm 1 \\ 49 \pm 0.3 \end{array}$	$\begin{array}{c} 434 \pm 11 \\ 315 \pm 1 \\ 35 \pm 1 \\ 29 \pm 1 \end{array}$	$\begin{array}{c} 124\pm1\\ 338\pm2\\ 43\pm0.5\\ 40\pm0.2 * \end{array}$	$\begin{array}{c} 514 \pm 4 \\ 332 \pm 0.2 \\ 39 \pm 0.5 \\ 34 \pm 0.3 \end{array}$	$\begin{array}{c} 400 \pm 9 \\ 314 \pm 1 \\ 31 \pm 0.5 \\ 27 \pm 1 \end{array}$	$\begin{array}{c} 102\pm 1\\ 335\pm 1\\ 41\pm 0.4\\ 37.5\pm 0.2\ ^*\end{array}$	574 ± 3 331 ± 0.2 42 ± 1 38 ± 0.3

The provided peak output power and pulse width values include standard deviation (SD) errors. Slope and optical efficiency values incorporate errors from curve fitting and uncertainty propagation, respectively. The relatively low standard deviation (SD) values in the peak output power demonstrate the stability and minimal power fluctuation between different laser operation modes.

The unoptimized mirror reflectivity of M2 at 1047 nm and 1053 nm limits the efficiency values achieved at these wavelengths. One could increase their efficiencies simply by exchanging the order of placement of M2 and M3, but at the cost of the high-efficiency emission at 1314 nm.

The M² value was measured by the knife edge technique using 10/90 clip levels and a correction factor of 1.561 to calculate the beam waist at $1/e^2$ [43,44]. Figure 6 shows the measured and corrected beam waist of the 1314 nm emission as a function of the distance from a spherical focusing lens with f = 40 mm. A similar curve fit was used to determine the M² for wavelengths at the 1.05 µm region.



Figure 6. Beam waist curve fit made by utilizing the Knife Edge Technique in the x in y axis, respectively.

These M^2 measurements were made for each wavelength during simultaneous triple wavelength operation with near equal amplitude. To separate the beams, a combination of a high-pass filter at 1.3 µm (Thorlabs, FELO1300), a HR mirror for 1.3 µm with high transmission at 1.05 µm, and a polarizer to isolate the emissions of the 1.05 µm emission were employed. For each wavelength, horizontal and vertical values were measured, all of which are shown in Table 3.

Wavalanath	M ²		
wavelength	x	у	
1314 nm	4.2 ± 0.1	2.93 ± 0.4	
1047 nm	2.4 ± 0.3	2.2 ± 0.4	
1053 nm	4.1 ± 0.2	2.4 ± 0.1	

Table 3. M^2 values 1047 nm, 1053 nm, and 1314 nm wavelengths.

Compared to other simple single-bounce, diode-pumped Nd:YLF lasers operating in the 1 μ m region, the achieved M_x² values of 2.4 at 1047 nm and 4.1 at 1053 nm perform well [25,31]. The M² values obtained for 1314 nm emission fare well when compared with similar compact cavities, especially considering the absence of any configuration for beam quality improvements, such as a DBMC or a larger resonator with intracavity cylindrical lenses [28].

The advantage of achieving efficient triple-wavelength emission, without the need for additional optical elements within the cavity, holds great value in the development of compact, cost-effective, and versatile lasers suitable for a wide range of applications. This is particularly evident in its application within χ^2 nonlinear phenomena, including Second Harmonic Generation, Sum Frequency Generation, and Difference Frequency Generation. These nonlinear processes allow for wavelength transformations, leading to a diverse range of multichromatic visible- and near-infrared (NIR) radiation, producing frequencies as low as 1.6 THz, using DFG for the 1047 + 1053 nm emission, and extend to 58 THz by employing SFG for the 1047 + 1314 nm emission, for example. Furthermore, although considerably more challenging, nonlinear transformations with triple-wavelength emission have the potential to generate radiation up to the 800 THz range when combined with SFG.

4. Conclusions

Simultaneous triple-wavelength emission at 1047 + 1053 + 1314 nm of a side-pumped Nd:YLF laser in a simple and compact cavity is presented for the first time. The wavelength selection of single, double, and triple-wavelength operation was made exclusively by cavity alignment and delivered a record slope and optical-to-optical efficiency of 53% and 49%, respectively, when optimized for the single 1314 nm emission, representing the highest efficiency achieved at this wavelength while pumped at 797 nm. Meanwhile, other wavelength operations remained, in all cases, above 31% of slope efficiency.

The beam qualities of all three wavelengths fare well when compared with related works. However, they could be further improved by employing techniques such as doublebeam mode controlling the cavity or increasing the crystal's laser mode size by applying cylindrical intracavity lenses. The resonator shows good promise for passive Q-switch applications, especially with broadband saturable absorbers such as V³⁺:YAG. The high-peak power multichromatic emission could facilitate the operation of a compact, multi-wavelength laser in the visible NIR and infrared by using non-linear processes such as SHG, DFG, and SFG.

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