# Application of multivariate calibration for simultaneous determination of major and minor constituents in $U_3Si_2$ by WDXRF technique

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**Abstract** The aim of this work was to implement and to validate the multivariate calibration for simultaneous determination of major and minor constituents in uranium nuclear fuel by WDXRF technique. The method is non-destructive and involves no chemical treatments thus is possible to perform fast chemical analysis and produces no hazardous waste. The precision and accuracy achieved are statistically comparable to others sensitive techniques like ICP-OES for impurities determination.

**Keywords**  $U_3Si_2 \cdot Elemental analysis \cdot Wavelength dispersive X-ray fluorescence <math>\cdot$  Multivariate calibration

### **Abbreviations CAS**

MTR	Material testing reactor
FP	Fundamental parameters
SDV	Singular value decomposition method
NBL	New brunswick laboratory
IPEN/	Instituto de Pesquisas Energéticas e
CNEN-SP	Nucleares
ICP-OES	Inductively coupled plasma optical
	emission spectrometry
RMB	Brazilian multipurpose reactor
FAAS	Flame atomic absorption spectrometry
PDCA	Pyridine-2,6-dicarboxylic acid
WDXRF	Wavelength dispersion X-ray fluorescence
ISO/IEC	General requirements for the competence
17025	of testing and calibration laboratories

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CRM	Reference materials characterized for
	uranium matrix impurities
RSD	relative standard deviation
RE	relative error
Z	Z-score
LoQ	Limit of quantification
MATLAB	Matrix laboratory
PC	Principal component
PLS	Partial least square
PCA	Principal component analysis

# Introduction

The first multi-purpose research nuclear reactor in Brazil (RMB) will become operational in 2018. As its name implies, the equipment, estimated at US \$500 million, has multiple purposes. These purposes include production of radioisotopes for use in nuclear medicine for cancer exams/ treatment and for research in the fields of nuclear technology, energy, agriculture, industry, materials science, and environment [1]. The technology to manufacture fuel for the RMB is already in place. The fuel will be plate type MTR, with an U<sub>3</sub>Si<sub>2</sub> base, and produced at the IPEN/CNEN-SP [1, 2]. Currently, the production of MTR fuel begins by mixing aluminum with uranium silicide powder enriched to 20 wt%

 $^{235}$ U, in proportions predetermined. After, the mixture is compressed as briquettes and degassed under vacuum. Finally, one set of U<sub>3</sub>Si<sub>2</sub>-Al briquettes is mounted on laminate to constitute the fuel core, which is then encased in a frame with two revetments of aluminum (top and nether). To ensure quality, stringent tests are applied at all process stages [3]. Although not an innovative technology, U<sub>3</sub>Si<sub>2</sub>, with 4.8 g U cm<sup>-3</sup>, is currently the world's most advanced commercial fuel [3]. Its performance in reactors depends on the chemical composition and absence of impurities. Lack of impurities is a requisite for good neutron economy, because their presence compromises the fuel energy density. Elements with a high neutron capture cross section, such as B and Cd, absorb thermal neutrons. The alkali, alkaline earth, and transition metals can form oxides, modifying the metal to oxygen ratio in a fuel matrix. Moreover, when combined with even ultra-trace levels of rare earth elements, such as Sm, Eu, Gd, and Dy, a decrease in energy density is caused, since radionuclides can be produced after reactor irradiation [4]. There are many techniques to determine impurities in uranium compounds. Spectroscopic methods are used most often because they allow for simultaneous determination using a small sample amount. These methods present advantages and disadvantages based on spectral interferences, accuracy, cost, type of sample (solid or liquid), and equipment used for analysis. The method must take into consideration the detection limit, sample preparation, and steps required for pre-concentration [4]. No single analytical technique is ideal for determination of all the elemental impurities since most of the elements are present in ultratraces levels, and sometimes techniques do not possess the detection limit required for determination of the analytes. Low concentrations of the impurities, in the range of mg  $g^{-1}$ to  $\mu g g^{-1}$ , associated with uranium complex matrices as UO<sub>2</sub>, U<sub>3</sub>Si<sub>2</sub>, U<sub>3</sub>O<sub>8</sub>, and U-Mo, need to be determined, and compatible analytical methodologies must to be validated **[4]**.

Thus, there is a need to develop rapid and simple methods for chemical characterization of materials used as nuclear fuel. In this context, the aim of this work is to evaluate the potential of WDXRF technique for chemical characterization of nuclear materials in accordance with technical specifications for nuclear fuels made of  $U_3O_8$  and  $U_3Si_2$ . The overall goal is to establish and validate a method for a non-destructive, inexpensive, and rapid quantitative chemical analysis, in addition to minimizing the generation of waste from simultaneous determination of the major constituents  $U_{total}$  and Si and impurities B, Mg, Al, Cr, Mn, Fe, Co, Ni, Cu, Zn, Mo, Cd, and others present in  $U_3O_8$  and  $U_3Si_2$  in accordance with ISO/IEC 17025.

### Materials and methods

### Sample preparation

compacted by a hydraulic press (Herzog) using a pressure of 20 MPa for 2 s on a base of boric acid (H<sub>3</sub>BO<sub>3</sub> PA) previously compressed with 100 MPa for 10 s. This gave pressed samples  $25.01 \pm 0.01$  mm in diameter and  $5.0 \pm 0.2$  mm in thickness.

### Instrumental parameters

The experiments were carried out using a WDXRF spectrometer RIGAKU Co., model RIX 3000 with X-ray tube a Rh anode, a 75 µm Be window, and a 60 kV maximum acceleration voltage, scintillation detector NaI(Tl) and flow-proportional counter. A deconvolution method was applied to correct for overlap U-L $\beta$ 1-2nd with Zn-K $_{\alpha}$ , UL $\beta$ 1 with Mo-K $_{\alpha}$ . Zr-filter for separation of the Rh-K $\beta$ 1 from Cd-K $_{\alpha}$  X-rays. The FP method was applied for correction of the absorption/excitation effects. The parameters such as excitation, emission line, divergence slit, diffracting crystal, detector, fixed counting time, and Bragg's positions for B, Mg, Al, Si, Ca, V, Cr, Mn, Fe, Co, Ni, Cu, Zn, Mo, Cd, Sn, Ba, Pb, and U are shown in Table 1.

# Reference materials

The two sets of reference materials characterized for uranium matrix impurities were from the New Brunswick Laboratory (NBL) and labeled CRM 123 (1–7) and CRM 124 (1–7) and one set of the sixteen  $U_3Si_2$  reference samples 20 % enriched in <sup>235</sup>U from the Nuclear Fuel Center of IPEN/CNEN-SP.

# Univariate calibration

First, a qualitative analysis was performed on CRM-124 (1) to check for interferences and set up instrumental conditions. The overlaps were corrected using filters and a deconvolution method with software coupled to the spectrometer.

$$I_{ic} = I_i \sum L_{ij} I_{ij} \tag{1}$$

where  $I_{ic}$  is the intensity after overlap correction,  $I_i$  intensity before overlap correction,  $L_{ij}$  overlap correction coefficient for element *j*, and  $I_{ij}$  is the intensity of element *j*.

The matrix correction coefficients (absorption/excitation) were calculated by the FP method [5] using software coupled to the spectrometer.

$$W_{i} = (aI_{i} * I_{i} + bI_{i} + C)$$

$$\left\{1 + K + \sum A_{ij}F_{j} + \sum Q_{ij}kF_{j}Fk + \sum \frac{RijFj}{1 + W1} + \sum B_{ij}F_{j} + \sum D_{ij}kF_{j}Fk + C\right\}$$

$$(2)$$

Table 1         Measurement
conditions for WDXRF-
Excitation: 50 kV $\times$ 50 mA

Elements	Emission line	Divergence slit (µm)	Diffracting crystal	Detector	Time (s)	Bragg's positions (°)
В	B-K <sub>α</sub>	560	RX70	FPC	200	49.280
Mg	Mg–K <sub>α</sub>	560	TAP	FPC	200	45.190
Al	Al- $K_{\alpha}$	560	PET	FPC	40	145.220
Si	Si-K <sub>a</sub>	560	PET	FPC	40	109.235
Ca	Ca-K <sub>α</sub>	560	Ge	FPC	40	61.260
V	$V-K_{\alpha}$	560	LiF(200)	SC	40	76.910
Cr	Cr-K <sub>a</sub>	560	LiF(200)	SC	20	69.330
Mn	$Mn-K_{\alpha}$	560	LiF(200)	SC	20	62.950
Fe	$Fe-K_{\alpha}$	160	LiF(200)	SC	20	57.505
Co	Co-K <sub>a</sub>	560	LiF(200)	SC	20	52.770
Ni	Ni-K <sub>a</sub>	160	LiF(200)	SC	20	48.650
Cu	Cu-K <sub>a</sub>	560	LiF(200)	SC	20	45.010
Zn	$Zn$ - $K_{\alpha}$	160	LiF(200)	SC	20	41.780
Мо	Mo-K <sub>α</sub>	560	LiF(200)	SC	20	20.320
Cd (F-Zr)	$Cd-K_{\alpha}$	560	LiF(200)	SC	20	15.300
Sn	$Sn-K_{\alpha}$	160	LiF(200)	SC	20	14.030
Ba	Ba-L <sub>α</sub>	560	LiF(200)	SC	20	87.130
Pb	$Pb-L_{\alpha}$	560	LiF(200)	SC	20	33.915
U	$U-L_{\alpha}1-2nd$	560	LiF(200)	SC	20	53.765

TAP thallium acid phtalate, PET pentaerythritol, LiF lithium fluoride, Ge germanium, SC scintillation detector, NaI(Tl): FPC flow-proportional counter, F-Zr Zr primary X-ray filter

where  $W_i$  is the quantification value, a, b, and c are calibration curve coefficients,  $I_i$  is the X-ray intensity, K constant term,  $A_{ij}$  absorption/excitation correction coefficient,  $F_j$  analysis value or X-ray intensity of correction component,  $Q_{ij}$  absorption/excitation correction coefficient (secondary correction),  $R_{ij}$  excitation correction coefficient,  $B_{ij}$  overlap correction coefficient,  $D_{ij}$  absorption/excitation correction coefficient,  $C_{ij}$  absorption/excitation correction coefficient,  $B_{ij}$  overlap correction coefficient,  $D_{ij}$  absorption/excitation correction coefficient,  $R_{ij}$  absorption/excitation correction coefficient,  $B_{ij}$  absorption/excitation correction coefficient,  $R_{ij}$  absorption/excitation correction coefficient coefficient

After setting up the instrumental conditions, seven measurements for B, Mg, Al, Si, Ca, V, Cr, Mn, Fe, Ni, Cu, Zn, Mo, Cd, Sn, and Pb were performed on CRM-123 (1–7). The net intensities of each element were related to their respective concentrations, and using linear regression the coefficients of each curve were calculated.

The methodology was evaluated using CRM-124(1). Three samples were prepared, and six measurements for each element were performed. The statistical tests were then applied.

At first, Chauvenet's test was applied for detection of outliers [5].

$$\left|X_{i} - \overline{X}\right| > k_{n} * s \tag{3}$$

where  $X_i$  is the individual measured value,  $\overline{X}$  average,  $k_n$  Chauvenet's coefficient, and s is the standard deviation.

The precision was calculated in terms of relative standard deviation (RSD) and accuracy in terms of relative error (RE) and Z-score (Z) [6].

$$Z = \frac{(\overline{X}_{\text{Lab}} - \overline{X}_{\text{CRM}})}{\sqrt{U_{\text{Lab}}^2 - U_{\text{CRM}}^2}} \tag{4}$$

where Z is the standard error,  $\overline{X}_{Lab}$  experimental average,  $\overline{X}_{CRM}$  certificate value,  $U_{Lab}^2$  experimental variance, and  $U_{CRM}^2$  is the certificate variance.

The limit of quantification (LoQ) was calculated according to Eq. 5 [6].

$$LoQ = 2 * \sqrt{\sum_{m=1}^{n} \frac{(C_m - \overline{C})^2}{n - 1}}$$
(5)

where  $C_m$  is the individual measured value,  $\overline{C}$  average, and n is the repetition number.

# Multivariate calibration

Under predetermined instrumental conditions, CRM-123 (1– 7) samples were measured in  $2\theta$  scan mode. The spectra and concentration of each element were organized in a matrix, X and Y, respectively. The mean vector; original matrix of autoscaled data; standard deviations vector of X variables; original matrix of autoscaled data; loadings matrix; scores matrix; singular values; vector regression parameters were calculated using MATLAB 7.0.1 [8]. The vector regression provided the multivariate calibration curve for U<sub>3</sub>O<sub>8</sub> samples. The methodology was evaluated using CRM-124 (1); three samples were prepared and six measurements were performed for each cited element. The same statistical tests described in Univariate calibration were applied.

The same process was applied to the  $U_3Si_2$  samples, and a multivariate calibration curve was obtained. The



Fig. 1 Cause and effect diagram showing sources of uncertainty associated with methods

quantification limit was calculated according to Eq. 5. The results obtained were compared with results from gravimetric for Si, volumetric for  $U_{total}$ , and ICP-OES for impurities methods, using analysis of variance ANOVA to determine precision and the student *t* test (paired *t* test), at a 0.5 significance level, to determine accuracy.

$$t_{\text{experimental}} = \frac{(d - d_0)}{sd/\sqrt{n}} \tag{6}$$

where d is the sample mean,  $d_0$  the mean value of differences in population tested, sd standard deviation of differences in populations, and n is the sample size.

### Uncertainty evaluation

The sources of error associated with analytical procedures that can influence the analytical results are represented in a cause and effect diagram (Fig. 1).

The diagram shows that uncertainty sources related to sample preparation and instrumental parameters are independent. Thus, the uncertainty of the method was calculated in terms of combined uncertainty  $(u_c)$  [9].

$$u_c = \sqrt{u_1^2 + u_2^2 + u_3^2 + \dots + u_n^2}$$
(7)

where  $u_c$  is the combined uncertainty, $u_1^2$  uncertainty of source 1,  $u_2^2$  uncertainty of source 2, and  $u_3^2$  is the uncertainty of source 3.

# **Results and discussion**

The qualitative analysis results for CRM-124 (1) (Fig. 2) showed overlaps of U-L $\beta$ 1-2nd with Zn-K $_{\alpha}$ , UL $\beta$ 1 with Mo-K $_{\alpha}$ , and Rh-K $\beta$ 1 with Cd-K $_{\alpha}$ ; furthermore, the counting rate was low for lines corresponding to B-K $_{\alpha}$ , Mg-K $_{\alpha}$ , Al-K $_{\alpha}$ , Si-K $_{\alpha}$ , V-K $_{\alpha}$ , Cr-K $_{\alpha}$ , Mn-K $_{\alpha}$ , Cu-K $_{\alpha}$ , Zn-K $_{\alpha}$ , Cd-K $\beta$ 1, and S-K $_{\alpha}$ . A deconvolution method was applied to correct for overlap, with the exception of Cd-



Fig. 2 WDXRF spectrum for CRM 124 (1)

 $K_{\alpha}$  where a Zr-filter was used. Subsequently, the FP method was applied for correction of the absorption/ excitation effects.

# Univariate calibration results

In Table 2, certified and determined values, RSD, RE, LoQ, and Z-score for MRC 124 (1)-NBL are presented, along with the correlation coefficients of the univariate calibration curves. The correlation coefficients for B (0.01), V (0.06), and Cd (0.17) are less than 1.00, indicating little a correlation between counting rate and concentration. The most likely hypothesis for any discrepancy is that the FP method used for absorption/excitation corrections was not effective, and that the Zr-filter used to correct the overlay of Rh-K $\beta$ 1 on Cd-K $_{\alpha}$  was also ineffective. Al (0.81), Mn (0.75), and Pb (0.81) are closer to 1.00, but still not satisfactory for the statistical tests applied. Thus, this methodology does not allow for quantification of B, Al, V, Mn, Cd, and Pb in the U<sub>3</sub>O<sub>8</sub> matrix. The elements with correlations >0.91, Mg, Si, Ca, Cr, Fe, Ni, Cu, Zn, Mo, and Sn had relative standard deviation values between 5 and 13 %, except for Mg (21 %). The accuracy in terms of relative error is <10 % for Mg, Ca, Cr, Ni, Zn, Sn, and Mo, whereas Si, Fe, and Cu had larger errors (56, 55, and 29 %). However, there are no statistically significant differences between the determined and certified values since Z-score values <2 for all elements, except Fe (Z = 4.8). This methodology is sensitive to impurities determination, with respect to the LoQ, since Si, Ni, Mo, and Sn are quantified at  $<10 \ \mu g \ g$  $^{-1}$ ; Ca, Cr, and Fe at <20 µg g $^{-1}$ ; and Mg, Cu, and Zn at  $<30 \ \mu g \ g^{-1}$ . Thus, Univariate calibration allows quantification of Mg, Si, Ca, Cr, Ni, Cu, Zn, Mo, and Sn impurities in U<sub>3</sub>O<sub>8</sub> matrices.

**Table 2** Certified anddetermined values for CRM 124(1) of the univariate calibrationcurves

Elements

В

Mg

A1

Si

Ca

V

Cr

Mn Fe

Ni

Cu

Zn

Mo

Cd

Sn

Pb

Xcert  $\pm \sigma$  (µg g<sup>-1</sup>)

 $5.1 \pm 1.0$ 

 $101 \pm 13$ 

 $205 \pm 37$ 

 $202 \pm 58$ 

 $200 \pm 36$ 

 $50.0 \pm 7.2$ 

 $102 \pm 14$ 

 $51.0 \pm 7.6$ 

 $210 \pm 24$ 

 $202 \pm 17$ 

 $50.0 \pm 9.4$ 

 $202 \pm 57$ 

 $100.0 \pm 5.5$ 

 $5.20\pm0.88$ 

 $51.0 \pm 6.9$ 

 $51 \pm 15$ 

Xdet  $\pm \sigma$  (µg g<sup>-1</sup>)

ND

ND

ND

ND

 $105 \pm 22$ 

 $89 \pm 4$ 

 $194 \pm 11$ 

 $108 \pm 8$ 

 $95 \pm 10$ 

 $191 \pm 1$ 

 $64 \pm 7$ 

RSD (%)

NC

21

NC

5

6

NC

7

NC

11

1

11

RE (%)

NC

4

NC

56

3

NC

6

NC

55

5

29

LoQ ( $\mu g g^{-1}$ )

NC

36

NC

9

13

NC

13

NC

21

2

34

*Xcert*  $\pm \sigma$  certified values, *Xdet*  $\pm \sigma$  determined values, *RSD* relative standard deviation, *RE* relative error, *LoQ* limit of quantification, *Z* Z-score,  $r^2$ correlation coefficients, *ND* not determined, *NC* not calculated



Fig. 3 Intensity versus energy plot used to obtain an X matrix with  $\rm U_3O_8\ CRMs$ 

# Multivariate calibration with U<sub>3</sub>O<sub>8</sub> CRM

The calibration model was constructed using the same set of MRC-123 (1–7) with the instrumental conditions presented in Table 1 using the  $2\theta$  scan method. The X matrix (intensity matrix) was obtained by averaging seven replicates for each element from all CRM measurements according to their respective energy (Fig. 3), resulting in a  $7 \times 19$  matrix. Using MATLAB 7.0.1 software, the mean



Fig. 4 Loading versus energy plot principal component PC1 in  $U_3O_8$  CRMs

values and deviations pertaining to the centering matrix were calculated. Subsequently, a principal component analysis was performed to determine the number of components needed to describe data set. The results showed a main component is sufficient (PC1 = 99.9999, PC2 = 0.0001 %) [10]. In Fig. 4, loading versus energy, calculated for PC1, is shown. Comparison of Figs. 3 and 4 indicates that one component is sufficient to describe the whole set. The calibration model was obtained using the partial least square (PLS) method [10], and statistical test validation was applied to CRM 124 (1).

In Table 3, certified and determined values, RSD, RE, LoQ, and Z-score are presented for CRM 124 (1) of the multivariate calibration. The precision assessment, in

 $r^2$ 

0.01

0.98

0.81

0.96

1.00

0.06

0.98

0.75

0.91

1.00

0.99

Ζ

NC

0.3

NC

1.9

0.2

NC

0.4

NC

4.8

0.6

1.5

Table 3 Certified and         determined values for CRM 124	Elements	Xcert $\pm \sigma$ (µg g <sup>-1</sup> ) (µg g <sup>-1</sup> )	Xdet $\pm \sigma ~(\mu g ~g^{-1})$	RSD (%)	RE (%)	$LoQ~(\mu g~g^{-1})$	Ζ
(1) of the multivariate calibration	В	$5.1 \pm 1.0$	$4.8 \pm 0.4$	8	6	2.6	0.3
	Mg	$101 \pm 13$	$82 \pm 7$	9	19	43	1.5
	Al	$205 \pm 37$	$166 \pm 14$	8	19	81	1.1
	Si	$202 \pm 58$	$197 \pm 16$	8	3	99	0.1
	Ca	$200 \pm 36$	$176 \pm 14$	8	12	87	0.7
	V	$50.0 \pm 7.2$	$40 \pm 4$	10	20	22	1.4
	Cr	$102 \pm 14$	$85 \pm 7$	8	17	43	1.2
	Mn	$51.0 \pm 7.6$	$42 \pm 4$	10	18	21	1.2
	Fe	$210 \pm 24$	$173 \pm 13$	8	18	80	1.5
	Ni	$202 \pm 17$	$169 \pm 12$	7	16	77	1.9
	Cu	$50.0 \pm 9.4$	$42 \pm 4$	10	16	22	0.8
	Zn	$202 \pm 57$	$179 \pm 15$	8	11	88	0.4
$V_{cart} + \sigma$ certified values	Мо	$100.0 \pm 5.5$	$85 \pm 1$	1	15	40	1.9
$Xdet \pm \sigma$ determined values, RSD relative standard deviation,	Cd	$5.20\pm0.88$	$4.2 \pm 0.4$	10	10	2	1.1
	Sn	$51.0\pm6.9$	$38 \pm 3$	8	25	20	1.8
<i>RE</i> relative error, <i>LoQ</i> limit of quantification, <i>Z</i> Z-score	Pb	51 ± 15	$35 \pm 3$	9	21	18	1.1

relation to the RSD, showed satisfactory repeatability for all elements determined (RSD <10 %). According to the INMETRO recommendation, RSD values above 10 % are considered unsatisfactory. The process was reproducible [9]. The accuracy evaluation, in relation to the Z-score, had values less than  $\leq 1.9$ , making it satisfactory [6]. The limits of quantification also showed adequate values once they were lower than 3  $\mu$ g g<sup>-1</sup> for B and Cd. Those elements are of great interest because of their high cross sections. Furthermore, for all other elements the LQ is less than 90  $\mu$ g g<sup>-1</sup>, with the exception of Si (99  $\mu$  g<sup>-1</sup>).

### Univariate and multivariate calibration comparison

The comparison between univariate and multivariate calibrations was made based on precision (RSD), accuracy (Z-score), and LoQ calculated for CRM 124 (1). The RSD (Fig. 5) for both methods is less than 10 %, except for Mg (21 %). Thus, it can be stated that the precision of the two methods is comparable. However, multivariate calibration has a higher precision for B, Mg, Al, V, Mn, Cd, and Pb determination. The Z-score values (Fig. 6) for both methods are <2, except for Cu (Z = 2.1) and Fe (Z = 4.8) using the univariate calibration. The results show that the accuracy of both methods is comparable; however, for Cu and Fe determination, multivariate calibration provides more reliable results (exact). Furthermore, for B, Al, V, Mn, Cd, and Pb, multivariate calibration has a greater accuracy. The LoQ (Fig. 7) is lower for Univariate calibration, except for Cu. However,



Fig. 5 RSD comparison of univariate and multivariate calibrations

multivariate calibration also has LoQ values sufficient for impurity determination in U<sub>3</sub>O<sub>8</sub> matrices.

Multivariate calibration using U<sub>3</sub>Si<sub>2</sub> reference samples

The calibration model based on the U<sub>3</sub>Si<sub>2</sub> samples was built in the same manner as the model for  $U_3O_8$ , i.e. the instrumental conditions presented in Table 2 using the  $2\theta$  scan method. The X matrix (intensity matrix) was also obtained by averaging seven replicas from each sample for each element, according to its respective energy (Fig. 8), resulting in a



Fig. 6 Comparison of the Z-score values for univariate and multi-variate calibration



Fig. 7 LoQ comparison for univariate and multivariate calibration

16 × 19 matrix. The PCA analysis revealed two principal components (PC1 = 99.982; PC2 = 0.016 %); however, PC1 is sufficient to describe the calibration model because it has the highest weight (~ 100 %). Loading versus energy is calculated for PC1 and shown in Figs. 9. 8 and 9 have similarities, proving that one component is sufficient to describe the whole range of the U<sub>3</sub>Si<sub>2</sub> samples, similar to U<sub>3</sub>O<sub>8</sub>. In Table 4, the U<sub>total</sub> and Si values were determined by conventional methods ( $\overline{X}_V$ : volumetric;  $\overline{X}_G$ : gravimetric). The B, Mg, Al, Si, Ca, V, Cr, Mn, Fe, Co, Ni, Cu, Zn, Mo, Cd, Ba, Sn, and Pb values were determined by ICP-OES ( $\overline{X}_{ICP-OES}$ ) and



Fig. 8 Intensity versus energy plot used to obtain an X matrix with  $U_3Si_2$  samples



Fig. 9 Loading versus energy plot for principal component PC1 in  $\mathrm{U}_3\mathrm{Si}_2$ 

WDXRF ( $\overline{X}_{MC-WDXRF}$ ) by multivariate calibration. Also, LoQ, F-distribution ANOVA, and the student *t* test to compare the difference in outcomes are all presented. The precision assessment, in relation to ANOVA, showed the three methods ( $\overline{X}_{V}$ : volumetric,  $\overline{X}_{G}$ : gravimetric,  $\overline{X}_{WDXRF}$ ) to be statistically equal. The F-distribution ANOVA calculated values were less than critical F-values for all the elements except Sn (F = 10.03,  $F_{critical} = 4.96$ ). The student *t* test for all the elements was also less than the critical *t* values. For the elements where the statistical tests did not apply B, Mo, Cd, and Ba, because the values were lower than the LoQ, a visual assessment demonstrated their compliance. The LoQ calculated for the multivariate calibration is sufficient for impurity determination in U<sub>3</sub>Si<sub>2</sub> and meets the specifications of U<sub>3</sub>Si<sub>2</sub> nuclear fuel.

Element	$\overline{X}_{ m V~(\%)}$	$\sigma^2$	$\overline{X}_{MC-1}$	WDXRF (%)	$\sigma^2$	LoQ	$_{(\mu g \ g)}^{-1}$	F	F critical	t	t <sub>critical</sub>	n
U	91.3	0.2	91.8		5.6	1		0.6	4.5	0.8	2.1	16
Element	$\overline{X}_{\mathrm{G}~(\%)}$	$\sigma^2$	$\overline{X}_{\mathrm{MC}}$	WDXRF (%)	$\sigma^2$	LQ	-1 (µg g)	F	F critical	t	t <sub>critical</sub>	n
Si	7.79	0.02	7.82		0.04	1		0.2	4.2	0.5	2.1	16
Elements	$\overline{X}_{ ext{ICP-OES}} \stackrel{-1}{}_{(\mu g)}$	<sub>g)</sub> c	$5^{2}$	$\overline{X}_{\text{MC-WDXR}}$	-1 F (μg g)	$\sigma^2$	LQ $_{(\mu g)}^{-1}$	<sub>g)</sub> F	F critical	t	t critical	n
В	1.5	1	.6	<4		NC	4	NC	NC	NC	NC	10
Mg	12.4	1	88.3	7.1		10.5	1	2.2	4.2	1.6	2.1	16
Al	260	1	28936	260		25022	23	0.1	4.2	0.1	2.1	16
Ca	11.8	1	47.2	10.0		42.4	1	0.3	4.2	0.7	2.1	16
V	1.8	5	.8	1.8		1.4	2	0.1	4.2	0.2	2.1	16
Cr	25	8	36	15		46	2	1.9	4.2	1.6	2.1	16
Mn	56	3	688	80		2591	8	0.2	4.2	1.0	2.1	16
Fe	283	5	3059	188		8647	12	2.3	4.2	0.1	2.1	16
Co	14	2		18		2	1	0.2	4.6	0.4	2.4	8
Ni	22	3	36	30		290	3	1.4	4.2	1.5	2.2	14
Cu	27	2	64	39		648	4	2.4	4.2	1.7	2.1	16
Zn	14	3	10	10		40	3	0.6	4.2	0.9	2.1	16
Мо	<3.0	Ν	ЧC	<1		NC	1	NC	NC	NC	NC	16
Cd	< 0.1	Ν	ЧC	<2		NC	2	NC	NC	NC	NC	12
Ba	< 0.2	Ν	ЧC	<10		NC	10	NC	NC	NC	NC	14
Sn	39	6	98	78		214	1	10.0	93 4.96	2.4	2.8	5
Pb	7.9	5	.6	9.4		0.4	1	1.3	7.7	1.1	4.3	3

Table 4 U<sub>total</sub>, Si and impurities values for U<sub>3</sub>Si<sub>2</sub> reference samples

 $\overline{X}$  Average,  $\sigma^2$  Variance,  $\overline{X}_V$  determined by volumetric method,  $\overline{X}_G$  determined by gravimetric method,  $\overline{X}_{ICP-OES}$  determined by ICP-OES method,  $\overline{X}_{WDXRF}$  determined by WDXRF methods, LoQ limit of quantification, F F-distribution value, t student t test value, n number of observations, NC not calculated

### Conclusions

The methodology proposed in this work would allow agencies to meet the requirements for nuclear materials control in relation to  $U_{total}$  and impurities in nuclear fuel that is based on  $U_3Si_2$ , enriched by 20 wt% <sup>235</sup>U, and  $U_3O_8$ , in accordance with ISO/IEC 17025. The method has minimal waste production, reducing analysis time and cost significantly. It also has promise as a method for chemical characterization of materials in nuclear fuel.

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